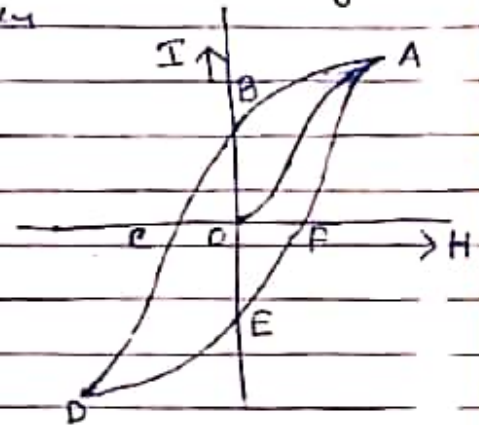


What do you mean by magnetic hysteresis and hysteresis loss? Show how is hysteresis related to the area of B-H loop.

Ans:- If a bar of iron is slowly magnetised, the intensity of magnetisation I increases with the magnetising field H as shown in fig. At A it reaches a saturation value, where any further increase in H would not increase I . The bar has acquired a state of magnetic saturation. Now the field H is decreased slowly to zero then I decreases but not become zero. This value of I is represented by OB and is called Residual magnetism or intensity of magnetisation or Retentivity or Remanence.

If the direction of H is now reversed, the curve BCD is obtained and residual magnetism vanishes at C . This is called coercive force of the material necessary to demagnetise the sample. By further increasing H we reach the saturation point D symmetrical to A and then it again decreases so as to reach the point A . The path $ABCDEFA$ is called hysteresis loop. This shows that the value of I or B always lags behind H .



This lagging of magnetic induction behind the magnetising force through a cycle of magnetisation is called Hysteresis.

Hysteresis loss is Energy loss due to hysteresis.

The act of magnetisation involves the expenditure of energy. The energy required to magnetise a specimen is not completely recoverable on reversing the magnetising field. Thus there is

a loss of energy and is represented by loop area of a hysteresis loop.

Hysteresis loss from I-H cycle:- let us consider a unit volume

of specimen containing N elementary magnets.
let M be the magnetic moment of one of the elementary magnet whose axis makes an angle θ with field H .

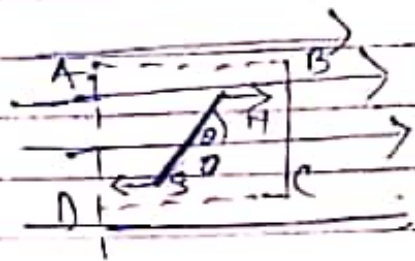
$$\begin{aligned} \text{Then component of } M \parallel \text{ to } H &= M \cos \theta \\ \text{" " " } M \perp \text{ to } H &= M \sin \theta \end{aligned}$$

Total mag. moment
parallel to H

$$= \sum M \cos \theta$$

and total moment \perp to H

$$= \sum M \sin \theta$$



when θ is increased by $d\theta$ then mag. moment
in per unit volume increases by

$$dI = d \sum M \cos \theta = - \sum M \sin \theta \cdot d\theta \quad \text{--- (1)}$$

The couple acting on each molecular magnet-

$$= MH \sin \theta$$

If the angle is decreased by angle $d\theta$, then work
done in rotating it = $- MH \sin \theta \cdot d\theta$.
it through $(-d\theta)$

∴ Work done in rotating all the magnets
in a unit volume = $-\sum MH \sin \theta \cdot d\theta$.

$$= H \cdot dI.$$

∴ the work done in changing the value of I

$$\text{from } I_1 \text{ to } I_2 = \int_{I_1}^{I_2} H \cdot dI \quad \text{(Waxburg's law)}$$

Loss of energy per cycle: Let us consider a complete cycle of magnetisation ABCDEFA.

Let PQ be the small step of magnetisation in which I increases by dI .

∴ Work done per unit volume = $H \cdot dI$

$$= \text{area } PARS$$

(1) when H is increased from 0 to L , I changes from $-OF$ to $+OM$ in specimen

∴ Work done per unit volume = $\int_E^M H \cdot dI$

$$= \text{area } EFAMBOE$$

(2) when H is decreased from L to zero, I decreases from OM to OB

∴ Work done per unit volume = $\int_M^B H \cdot dI = \text{area } AMBA$

(3) when H again changed in opposite direction from 0 to OL , I changes from $+OB$ to $-ON$

∴ work done on specimen per unit volume

$$= \int_B^N H \cdot dI = \text{area } BCDNEOB$$

(4) when H is again decreased to zero, I decreases from $-ON$ to $-OE$.

∴ Work done by specimen per unit volume

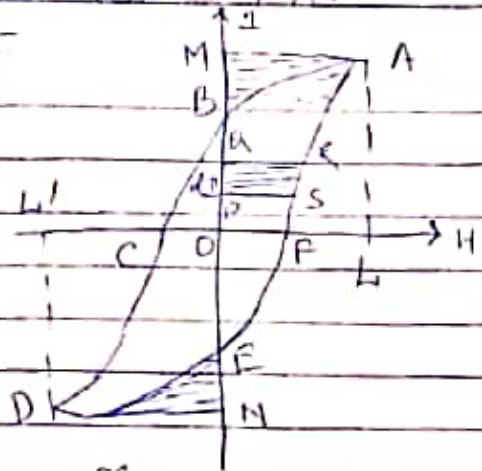
$$= \int_N^E H \cdot dI = \text{area } DNED$$

∴ Loss of energy per unit volume per cycle due to hysteresis = area of loop A

$$(\text{area } EFAMBOE + \text{area } BCDNEOB)$$

$$- (\text{area } AMBA + \text{area } DNED)$$

$$= \text{area of } \oint H \cdot dI \text{ loop } (ABCDEFA)$$



Hysteresis loss from B-H Curve

$$\text{We know } B = \mu_0(H + NI)$$

$$\therefore dB = dH + 4\pi NI$$

$$\therefore H dB = H dH + 4\pi NI dI$$

$$\therefore H dI = \frac{1}{4\pi N} (H dB - H dH)$$

$$W = \int H dI = \frac{1}{4\pi N} \int (H dB - H dH)$$

$$= \frac{1}{4\pi N} \int H dB$$

$$= \frac{1}{4\pi N} \text{ area of B-H curve}$$